

For assignment 1, we needed to match impedance with a parallel, transformer based circuit. If we continue the Lab 1 example, which we did at 1 MHz (note your results will be different at 8 MHz) we had found the input impedance to be  $Z_{in} = 323.771 - j872.113$ . To do a parallel match, need  $Y_{in} = 1/Z_{in}$

$$Y_{in} = \frac{1}{Z_{in}} = \frac{1}{323.771 - j872.113} = 0.374m + j1.008m$$

As an aside in case you have forgotten how to take the inverse of a complex number - Either (1) multiply top and bottom by the complex conjugate ( $323.771 + j872.113$ ) or (2) convert to magnitude and angle (930.273 angle -69.633 degrees), take the inverse of the magnitude (1.075m) and the negative of the angle (+69.633 degrees) convert back to rectangular ( $0.374m + j1.008m$ ) in agreement with the above.

$Y_{in}$  represents a parallel resistor (roughly equal to  $r_{\pi}$ ) parallel to a parallel capacitor (roughly equal to  $c_{\pi}$  gain  $\times c_{\mu}$ ).

$Y_{in} = 1/R_{amp} + j\omega C_{amp}$ , or  $R_{amp} = 2674\Omega$ , and  $C_{amp} = 160.0$  pF.

So, we will be matching  $50\Omega$  to  $2674\Omega$ , requiring a turns ratio of  $\frac{N_2}{N_1} = \sqrt{\frac{2674}{50}} = 7.313$

Now to get the correct bandwidth, the resistance seen on the  $N_2$  side of the transformer will be  $R_{amp}$  of 2674 Ohms and the transformed resistance from the 50 Ohm source which will transform to exactly 2674 Ohms so the resistance is  $2674/2$  or  $R_{total} = 1337$  Ohms.

Since  $BW = 1/R_{total}C_{total}$  and since the example shown happened to have 325 kHz bandwidth, let's do that here as well - of course, your bandwidth (and centre frequency) will be different. Thus,  $2\pi \times 325$  kHz =  $1/R_{total}C_{total}$  and  $C_{total}$  can be calculated to be 366 pF. Fortunately, this is bigger than  $C_{amp}$  thus we need to add  $C_{add} = 366 - 160 = 206$  pF.

Then, inductance L can be found from the required centre frequency knowing that

$$2\pi \times 1M = \frac{1}{\sqrt{LC_{total}}} \text{ or } L = \frac{1}{(2\pi \times 1M)^2 C_{total}} = 69.21\mu H$$

Now, the design is complete, except that we were supposed to take into account that all inductors, including the transformer have a Q of 50. Thus, knowing L, we can calculate the parallel resistance  $R_p = Q\omega L = 50 \times 2\pi \times 1M \times 69.21 \mu H = 21.68k$ . Thus we are trying to match to  $R_p \parallel R_{amp} = 2451\Omega$ .

Fortunately, this hasn't changed the numbers much, but that could be different in your case at 8 MHz. Now we need to go through the calculations again:  $R_{total} = 2451/2 = 1226$ .  $C_{total} = 399.4$  pF,  $L = 63.42$  uH. As a result the new  $R_p$  is 19.92k.

For the output transformer, we replace the load resistor  $R_L$  with  $50 \Omega$ , through a transformer with turns

$$\text{ratio } \frac{N_4}{N_3} = \sqrt{\frac{50}{R_L}} \text{ (in the original circuit, } R_L \text{ was } 3k).$$

Total Gain from source to output is:

$$A_v = \frac{1}{2} \frac{N_2}{N_1} g_m R_{LTotal} \cdot \frac{N_4}{N_3} \text{ where } R_{LTotal} = r_o \parallel R_L \parallel R_{3p}. \text{ Here } R_{3p} \text{ is the parallel resistance of the } N_3 \text{ side of the}$$

transformer. We are ignoring the inductance of the  $N_4$  side. Note, if input voltage is defined not as the source, but directly at the  $N_1$  side of the transformer, then the factor of  $1/2$  would be left out.

Bandwidth of the two circuits combined will be narrower and are given by the formula in the notes - result, new bandwidth is narrower by a factor of 0.6423, so new bandwidth is  $325 \times 0.6423 = 209$  kHz.